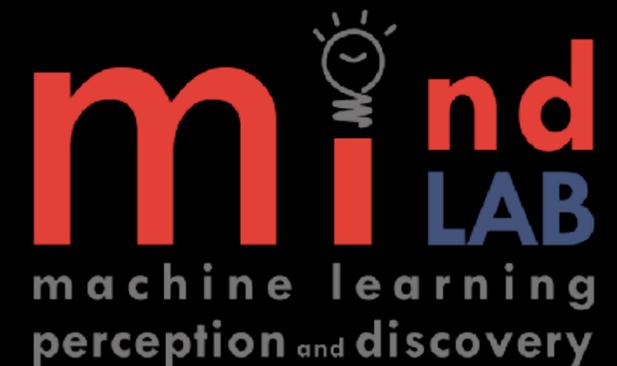
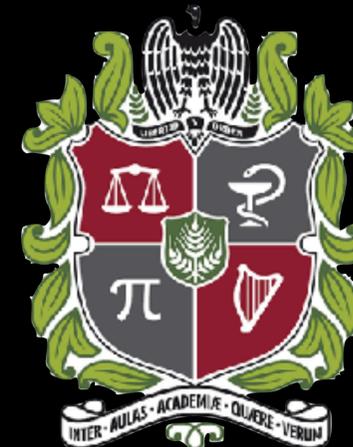


# Quantum Machine Learning

Fabio A. González

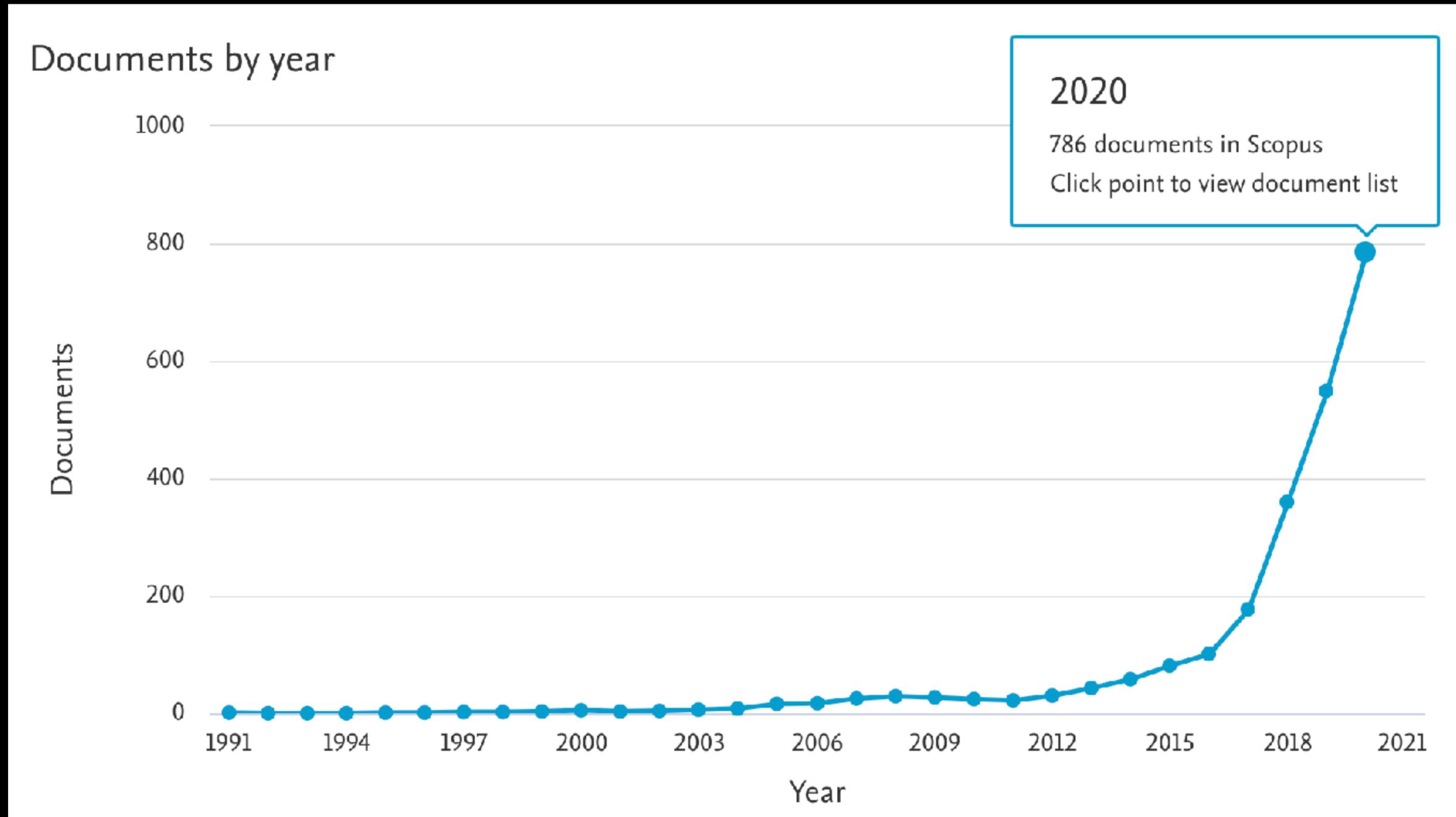
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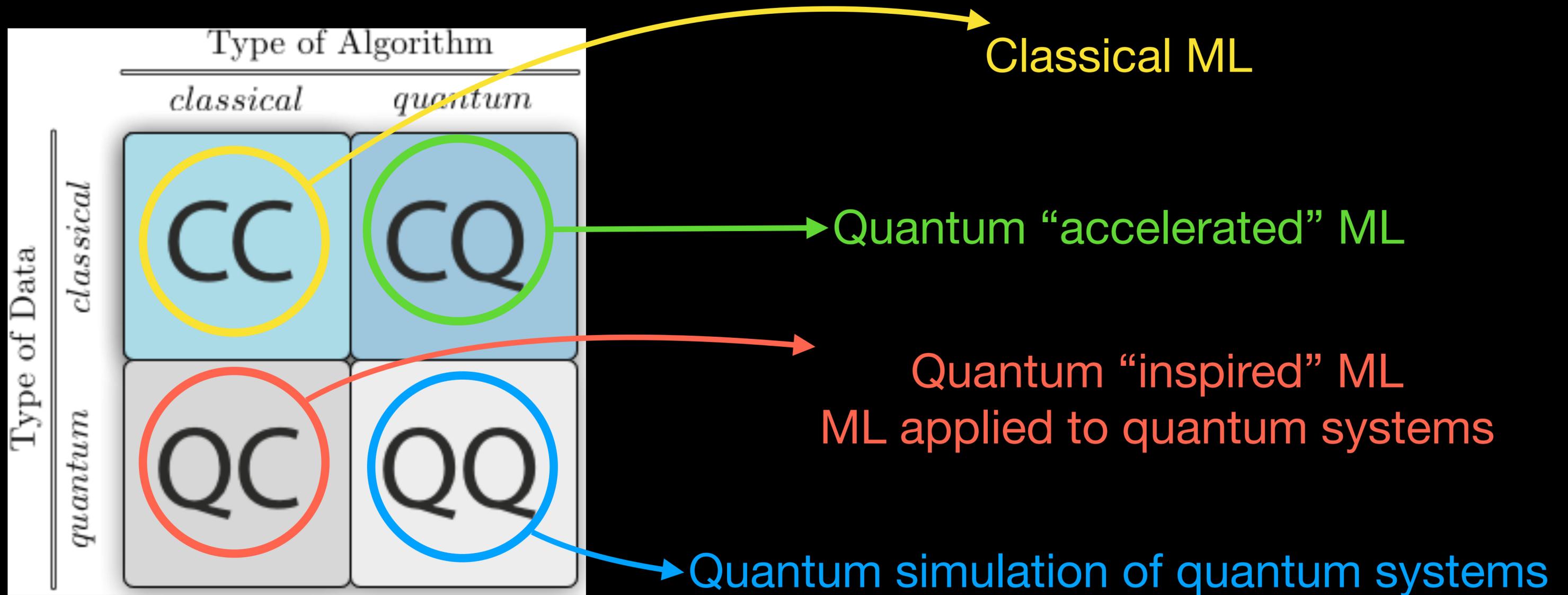
# Quantum machine learning

## Number of papers per year

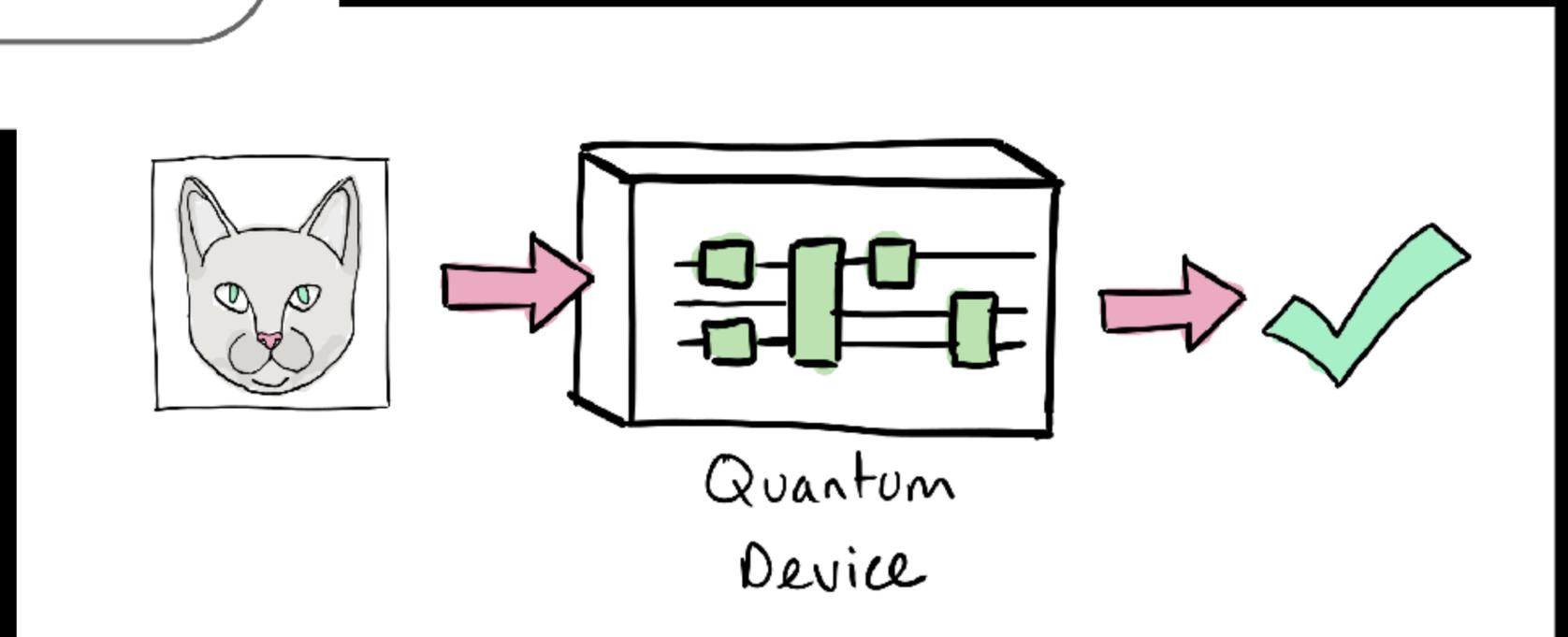
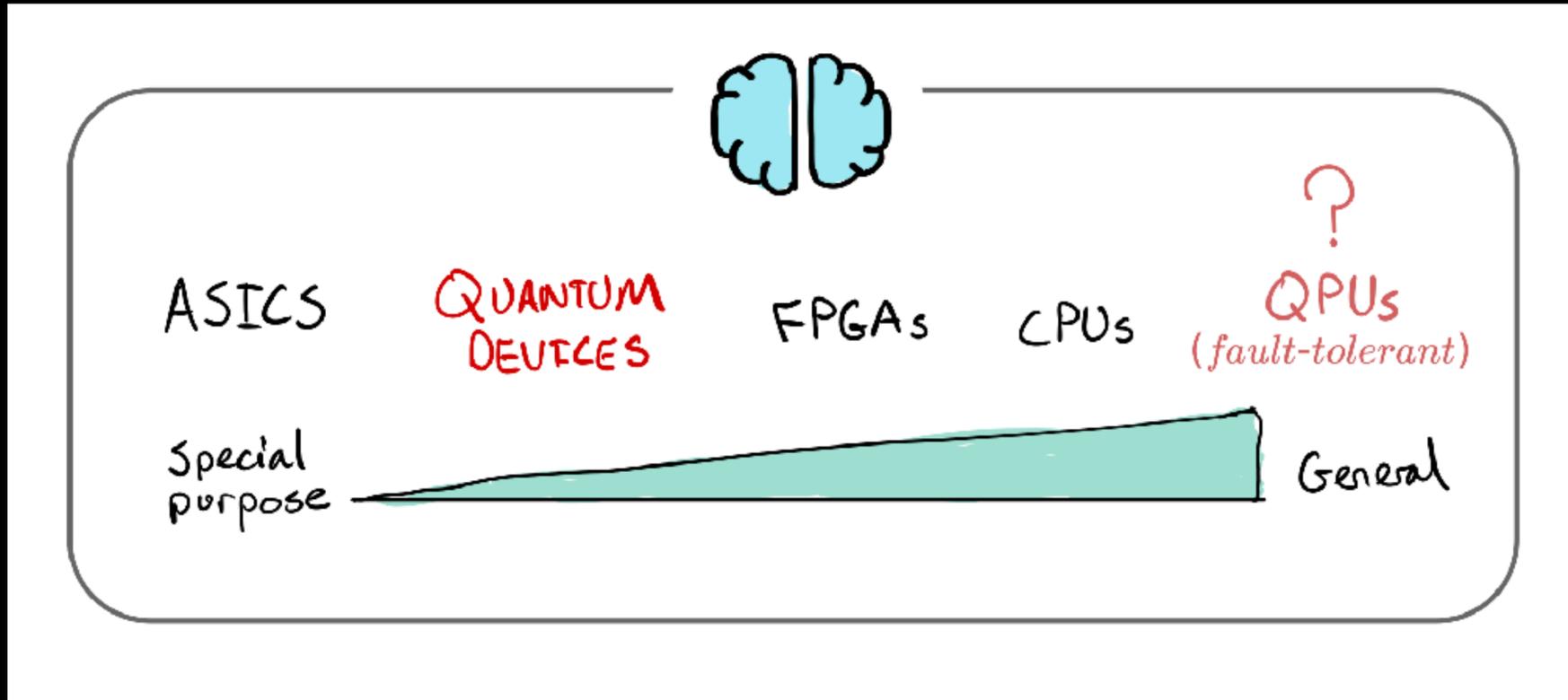


# Quantum machine learning

## Approaches

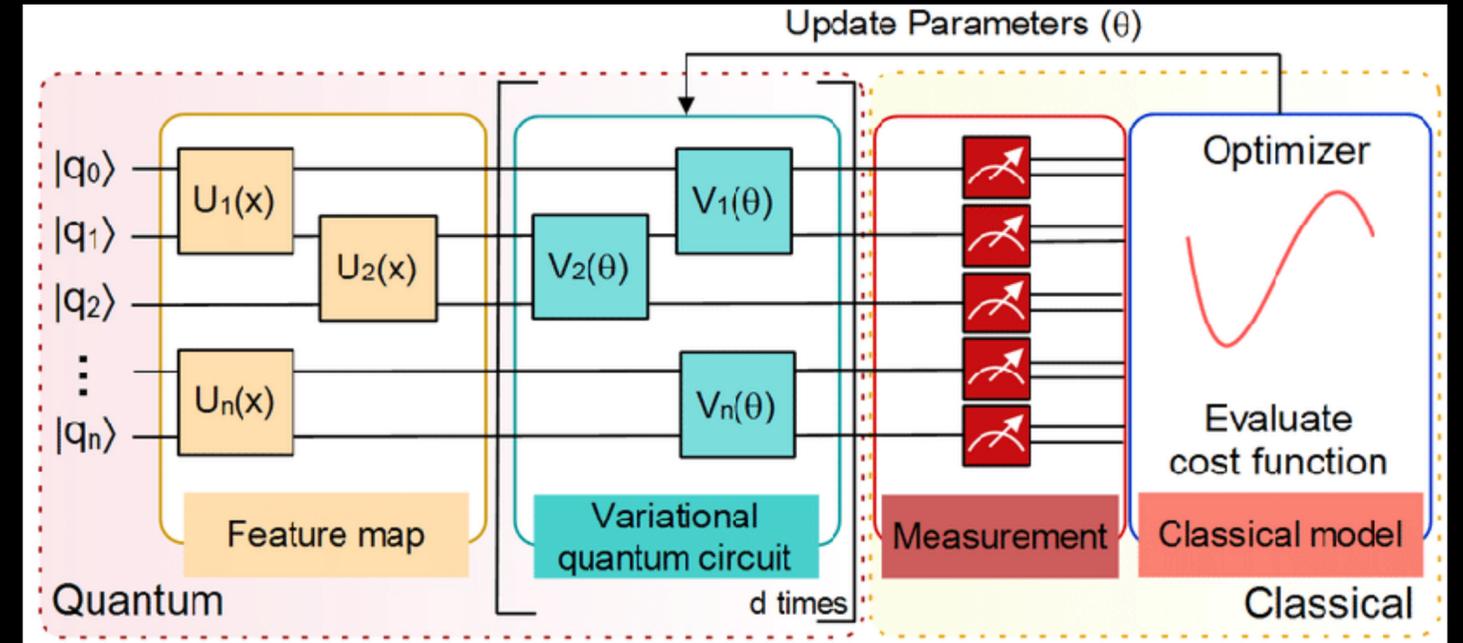


# Quantum “accelerated” ML



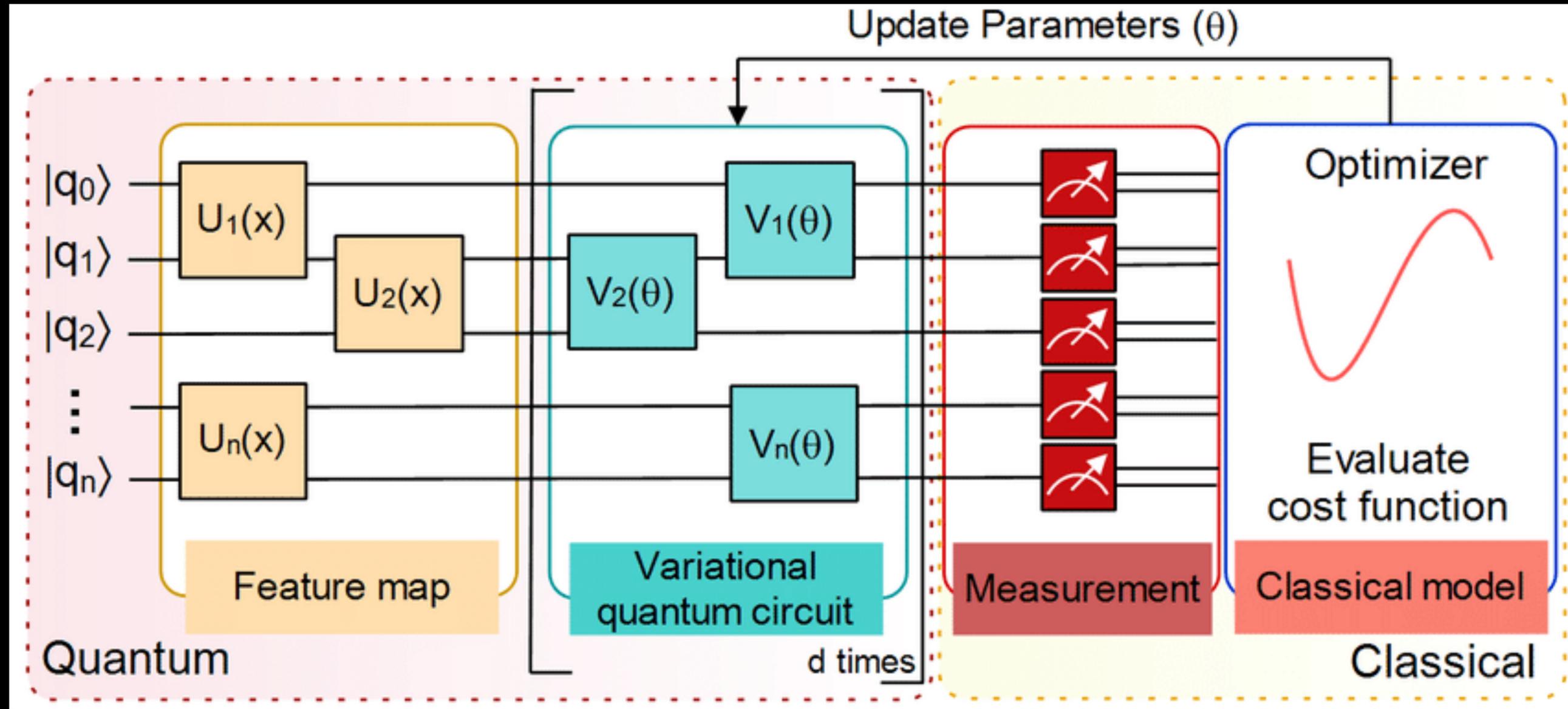
# Quantum “accelerated” ML Algorithms

- Variational classifiers
- Quantum kernels
- Quantum SVMs
- Quantum neural networks
- Quantvolutional neural networks
- Quantum GANs
- Etc.



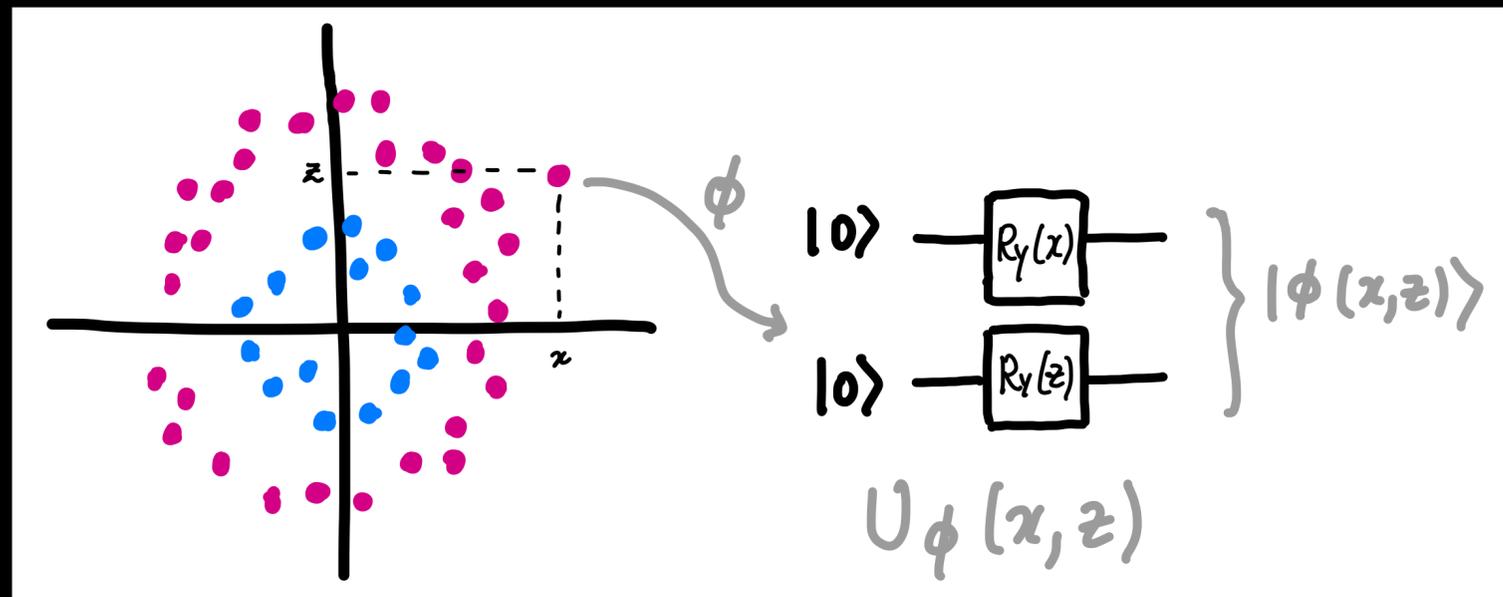
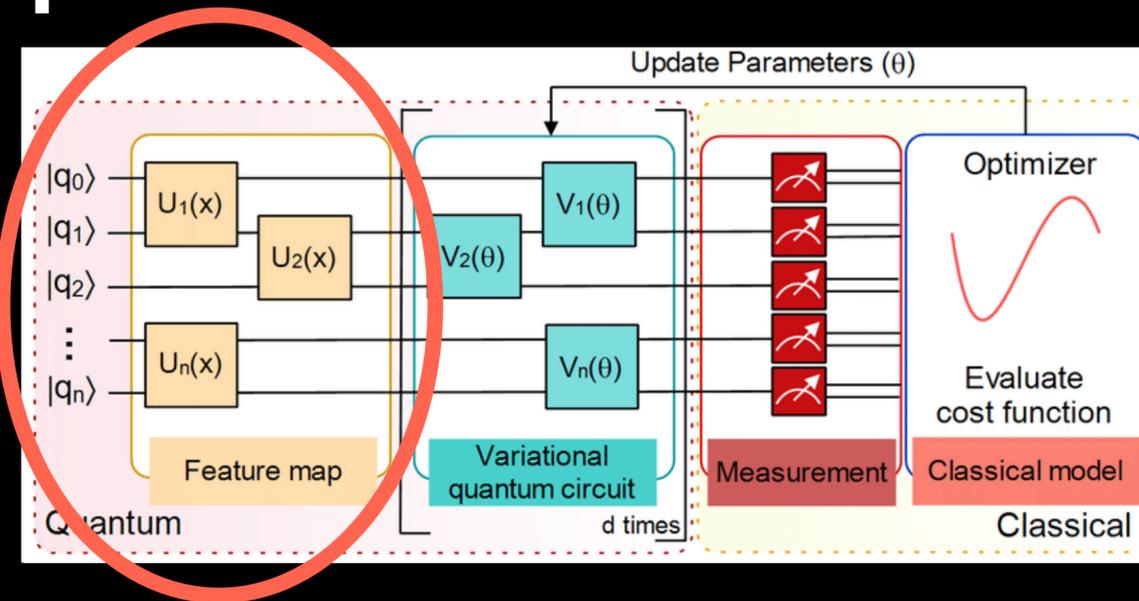
# Quantum “accelerated” ML

## Variational Classifier



# Quantum “accelerated” ML

## Quantum feature map



- Basis encoding
- Amplitude encoding
- Angle encoding
- Hamiltonian encoding

# Quantum “accelerated” ML

## Basis embedding

- Input dataset:

$$\mathcal{D} = \{x^{(1)}, \dots, x^{(m)}, \dots, x^{(M)}\}, x^{(i)} \in X^N$$

- Dataset is represented as superpositions of computational basis states:

$$|\mathcal{D}\rangle = \frac{1}{\sqrt{M}} \sum_{m=1}^M |x^{(m)}\rangle$$

- For binary variables requires  $N$  qubits

# Quantum “accelerated” ML

## Amplitude embedding

- A normalized classical  $N$ -dimensional datapoint is represented by the amplitudes of an  $n$ -qubit quantum state with  $N = 2^n$

$$|\psi_x\rangle = \sum_{i=1}^N x_i |i\rangle,$$

- The input examples are concatenated together

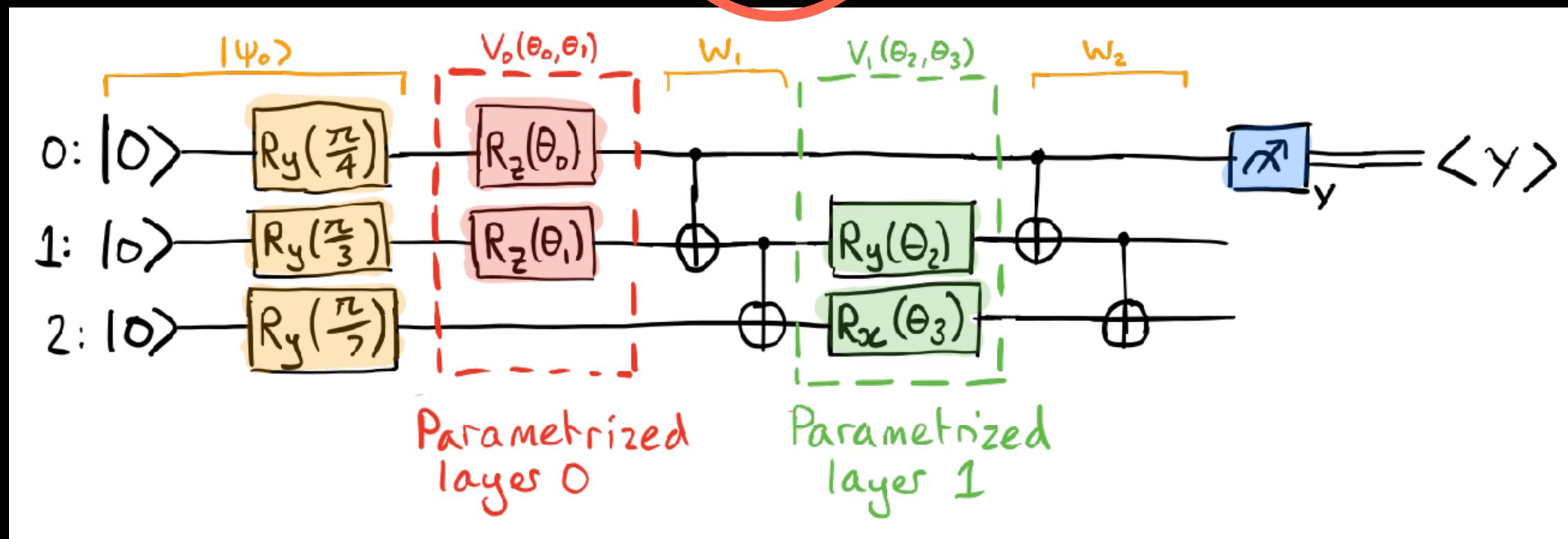
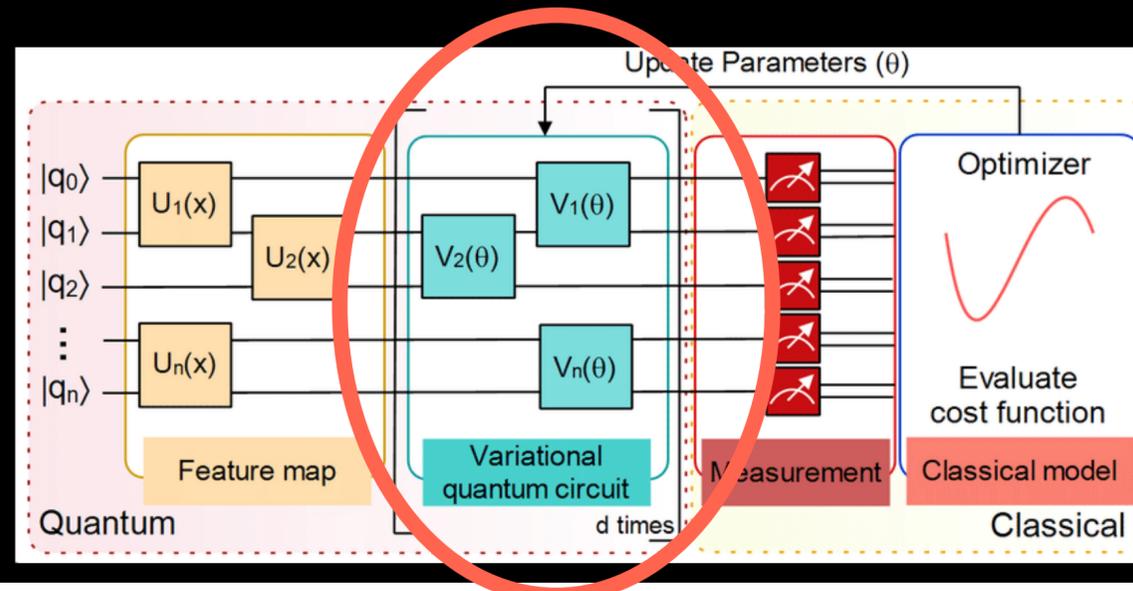
$$\alpha = C_{norm} \{x_1^{(1)}, \dots, x_N^{(1)}, x_1^{(2)}, \dots, x_N^{(2)}, \dots, x_1^{(M)}, \dots, x_N^{(M)}\},$$

- The dataset is represented as:

$$|\mathcal{D}\rangle = \sum_{i=1}^{2^n} \alpha_i |i\rangle,$$

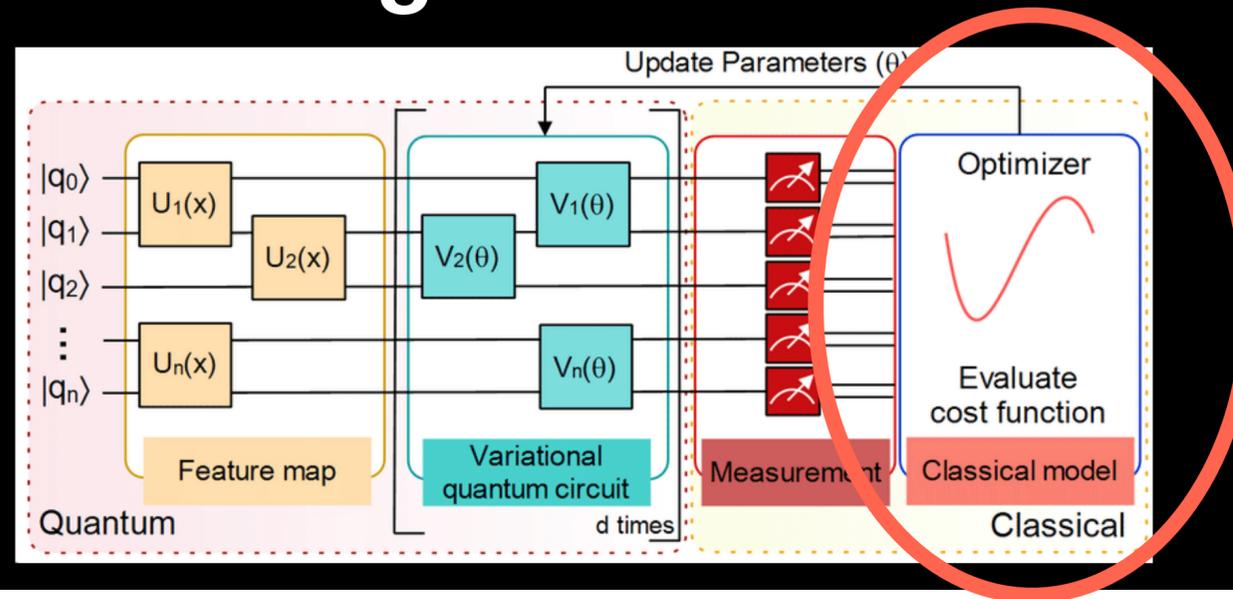
# Quantum “accelerated” ML

## Quantum circuit



# Quantum “accelerated” ML

## Parameter shift to calculate gradients



$$|0\rangle^{\otimes n} \longrightarrow U(\theta) \longrightarrow \text{Measurement} = \hat{y}_\theta$$

$$\text{Gradient} = |0\rangle^{\otimes n} \longrightarrow U(\theta + s) \longrightarrow \text{Measurement} = \hat{y}_{\theta+s} - |0\rangle^{\otimes n} \longrightarrow U(\theta - s) \longrightarrow \text{Measurement} = \hat{y}_{\theta-s}$$

# Quantum “accelerated” ML

## Parameter shift

- Objective function:

$$f(\theta) = \langle \psi | U_G^\dagger(\theta) A U_G(\theta) | \psi \rangle$$

- Parameterized gate with generator  $G$  (Hermitian):

$$U_G(\theta) = e^{-i\theta G} = I \cos(\theta) - iG \sin(\theta)$$

- If  $G$  has only two eigenvalues  $e_0$  and  $e_1$ , we have:

$$\frac{d}{d\theta} f(\theta) = r \left[ f\left(\theta + \frac{\pi}{4r}\right) - f\left(\theta - \frac{\pi}{4r}\right) \right] \quad r = \frac{a}{2}(e_1 - e_0)$$

# Quantum “accelerated” ML

## Parameter shift for Pauli gates

$$\begin{aligned} R_X(\theta) &= e^{-i\frac{1}{2}\theta X} & r &= \frac{1}{2} \\ R_Y(\theta) &= e^{-i\frac{1}{2}\theta Y} & r &= \frac{1}{2} \\ R_Z(\theta) &= e^{-i\frac{1}{2}\theta Z} & r &= \frac{1}{2} \end{aligned}$$

$$\frac{d}{d\theta} f(\theta) = \frac{1}{2} \left[ f\left(\theta + \frac{\pi}{2}\right) - f\left(\theta - \frac{\pi}{2}\right) \right]$$

Crooks, G. E. (2019). *Gradients of parameterized quantum gates using the parameter-shift rule and gate decomposition*. arXiv preprint arXiv:1905.13311

THE END

Gracias!

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